

# Statistics calculated on confusion matrix

## Confusion matrix

### Theoretical confusion matrix

		Automatic classification	
		<i>Positive</i>	<i>Negative</i>
Manual classification	<i>Positive</i>	TP	FN
	<i>Negative</i>	FP	TN

### Example

Automatic classification of three groups **A**, **B**, **C**

		Automatic classification		
		<i>A</i>	<i>B</i>	<i>C</i>
Manual classification	<i>A</i>	1	1	1
	<i>B</i>	1	3	0
	<i>C</i>	0	0	3

For group **A**, the matrix can be reduced as:

		Automatic classification	
		<i>Group A</i>	<i>Not group A</i>
Manual classification	<i>Group A</i>	TP = 1	FN = 2
	<i>Not group A</i>	FP = 1	TN = 6

For group **B**, the matrix can be reduced as:

		Automatic classification	
		<i>Group B</i>	<i>Not group B</i>
Manual classification	<i>Group B</i>	TP = 3	FN = 1
	<i>Not group B</i>	FP = 1	TN = 5

For group **C**, the matrix can be reduced as:

		Automatic classification	
		<i>Group C</i>	<i>Not group C</i>
Manual classification	<i>Group C</i>	TP = 3	FN = 0
	<i>Not group C</i>	FP = 1	TN = 6

## ***Explanation of main parameters***

### **TP : True Positive**

Number of particles of the group of interest correctly classified.

### **TN : True Negative**

Number of particles of all the other groups classified as other groups.

### **FP : False Positive**

Number of particles of other groups classified in the group of interest.

### **FN : False Negative**

Number of particles of the group of interest classified in the other groups.

## **General statistics**

### ***Accuracy***

$$\frac{(TP + TN)}{(TP + TN + FP + FN)}$$

### ***Error***

1 – Accuracy

## The eight basic ratios

### **Recall**

Also called: Sensitivity, TPR : True Positive Rate, Power, Probability of detection

$$\frac{TP}{(TP + FN)} = 1 - \text{FNR}$$

### **Specificity**

Also called: TNR : True Negative Rate, Selectivity

$$\frac{TN}{(TN + FP)} = 1 - \text{FPR}$$

### **Precision**

Also called: PPV : Positive Predicted Value, Reproducibility, Repeatability

$$\frac{TP}{(TP + FP)} = 1 - \text{FDR}$$

### **NPV : Negative Predicted Value**

$$\frac{TN}{(TN + FN)} = 1 - \text{FOR}$$

### **FPR : False Positive Rate**

Also called: alpha, Type I Error, p-Value

$$\frac{FP}{(FP + TN)} = 1 - \text{Specificity}$$

### **FNR : False Negative Rate**

Also called: beta, Type II Error

$$\frac{FN}{(TP + FN)} = 1 - \text{Recall}$$

### **FDR : False Discovery Rate**

Also called : q-Value

$$\frac{FP}{(TP + FP)} = 1 - \text{Precision}$$

**FOR : False Omission Rate**

$$\frac{FN}{(FN + TN)} = 1 - NPV$$

## The four ratios of ratios

### **LRPT : Likelihood Ratio for Positive Tests**

$$\frac{TP/(TP+FN)}{FP/(FP+TN)} = \frac{\text{Recall}}{(1-\text{Specificity})} = \frac{\text{Recall}}{\text{FPR}}$$

### **LRNT : Likelihood Ratio for Negative Tests**

$$\frac{FN/(FN+TP)}{TN/(TN+FP)} = \frac{(1-\text{Recall})}{\text{Specificity}} = \frac{\text{FNR}}{\text{Specificity}}$$

### **LRPS : Likelihood Ratio for Positive Subjects**

$$\frac{TP/(TP+FP)}{FN/(FN+TN)} = \frac{\text{Precision}}{(1-\text{NPV})} = \frac{\text{Precision}}{\text{FOR}}$$

### **LRNS : Likelihood Ratio for Negative Subjects**

$$\frac{FP/(FP+TP)}{TN/(TN+FN)} = \frac{(1-\text{Precision})}{(1-\text{FOR})} = \frac{\text{FDR}}{\text{NPV}}$$

## Additional statistics

### **Fmes : F-measure**

Also called: F1-score, harmonic mean of precision and recall

$$2 * \left( \frac{\text{Precision} * \text{Recall}}{\text{Precision} + \text{Recall}} \right)$$

### **BalAcc : Balanced accuracy**

$$\frac{(\text{Specificity} + \text{Recall})}{2}$$

### **MCC : Matthews Correlation Coefficient**

Attention: If any sum of the denominator is **0**, the total denominator can be set to **1**

$$\frac{(\text{TP} * \text{TN}) - (\text{FP} * \text{FN})}{\sqrt{((\text{TP} + \text{FP}) * (\text{TP} + \text{FN}) * (\text{TN} + \text{FP}) * (\text{TN} + \text{FN}))}}$$

### **Chisq : $\chi^2$**

Also called : Significance

$$\frac{[(\text{TP} * \text{TN}) - (\text{FP} * \text{FN})]^2 * (\text{TP} + \text{TN} + \text{FP} + \text{FN})}{(\text{TP} + \text{FP}) * (\text{TP} + \text{FN}) * (\text{TN} + \text{FP}) * (\text{TN} + \text{FN})}$$

### **Auto\_Manu : Difference between Automatic and Manual classification**

$$(\text{TP} + \text{FP}) - (\text{TP} + \text{FN})$$

### **Dissimilarity Index of Bray Curtis**

$$\frac{|(\text{Auto} - \text{Manu})|}{\sum (\text{TP} + \text{FP}) + \sum (\text{TP} + \text{FN})}$$